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l.Problem definition

2.Model and algorithm

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Problem definition

- Model and algorithm
- Experiments
- Conclusion







Problem definition

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Platform	 M heterogeneous processors N periodic atomic independent tasks Worst case execution time of task τ_i on processor m_k : c_{i,k} 		
Deadline	Tasks period: p		
Energy	 Static energy consumption of processor m_k used: E_{k,s} = P_{k,s} × p Dynamic energy consumption of task τ_i on processor m_k: E_d(τ_i, m_k) = P_{k,d} × c_{i,k} 		
Reliability	 Transient fault rate of processor m_k: λ_k Reliability of task τ_i on processor m_k: R(τ_i, m_k) = e^{-λ_k×c_{i,k}} Task τ_i needs to reach a reliability target R_i using replicas: R(τ_i) = 1 − Π_{k∈alloc(i)}(1 − R(τ_i, m_k)) ≥ R_i 		



Problem description

	- Determine for each task τ_i a set of replicas which are executed on a set of processors
Objective	- Build a schedule for each processor m_k
	 Minimize expected energy consumption, while matching the deadline p and reliability threshold R_i for each task

This is an **NP-Hard** problem!



Mapping strategies

Objective	Define the number of replicas for each task, as well as the execution processor for every replica		
	 Order all the tasks with one of the following criteria and renumber them τ₁, τ₂,, τ_N deW/inW: decreasing/increasing average WCET on all processors deMinW/inMinW: decreasing/increasing minimum WCET on all processors deMaxW/inMaxW: decreasing/increasing maximum WCET on all processors random: random ordering 		
Algorithm	 For each task τ_i in the list, Order all processors with one of the following criteria and renumber them m₁, m₂,, m_M inE: increasing energy cost deR: decreasing reliability deP: decreasing ratio of - log₁₀(1-R(τ_i,m_k))/E(τ_i,m_k) random: random ordering While the reliability target R_i is not reached, add replicas for task τ_i in the order of m₁, m₂,, m_M, skip 		
	the processor if already full		

Scheduling strategies

Objective	Order the replicas mapped on each processor, to minimize the energy consumption during execution		
Algorithm	 Order all the tasks with one of the following criteria and renumber them τ₁, τ₂,, τ_N deNR/inNR: decreasing/increasing number of replicas deU/inU: decreasing/increasing total utilization (sum up the ratio of c_{i,k}/p for all replicas of task τ_i) random: random ordering For each task τ_i in the list, identify a primary replica according to one of following criteria and schedule it as soon as possible on its assigned processor time: choose the replica that can complete the earliest on its processor energy: choose the replica that can be executed with the smallest dynamic energy With a round-robin fashion in the reversed list τ_N, τ_{N-1},, τ₁, choose a secondary replica of task τ_i (if exists) and schedule it as late as possible on its assigned processor time: choose the replica whose start time can be the latest energy: choose the replica that can be executed with the largest dynamic energy 		



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Parameters

Parameter	Description	Values
М	Number of processors	= 10
Ν	Number of tasks	= 20
р	Period and deadline of tasks	= 100
$\operatorname{cor}_{\operatorname{task}} / \operatorname{cor}_{\operatorname{proc}}$	Correlation of WCET values between the different tasks and processors	$= \{0, 0.25, 0.5, 0.75, 1\}$
$c_{i,k}$	Worst case execution time of task τ_i on processor \textbf{m}_k	Randomly generated with correlation
BasicWork	Estimation of the fraction of time that the platform is used if each task has a single replica	$=\frac{\sum_{i,k} c_{i,k}}{M^2 p} = \frac{\sum_{i,k} c_{i,k}}{M} \times \frac{1}{M p} = \{0.1, 0.2, 0.3\}$
$\beta_{b/w}$	Ratio between best case execution time and worst case execution time	$= \{0.2, 0.4, 0.6, 0.8, 1\}$
W _{i,k}	Actual execution time of task τ_i on processor $m_{\rm k}$	$[\beta_{b/w} \mathbf{c}_{i,k}, \mathbf{c}_{i,k}]$
$P_{k,s}$	Static power of processor m_k	= 0.001 (for all k)
P _{k,d}	Dynamic power of processor \boldsymbol{m}_k	[0.8, 1.2] (small failure rate case) [0.08, 0.12] (big failure rate case)
$\lambda_{k,d}$	Failure rate of processor \boldsymbol{m}_k	[0.0001, 0.00023] (small failure rate case) [0.01, 0.023] (big failure rate case)
R _i	Reliability target of task τ_{i}	{0.9, 0.92, 0.94, 0.96, 0.98} (small failure rate case) {0.8, 0.85, 0.9, 0.95} (big failure rate case)

• Large failure rate case and only representative results presented

 Comparison of our strategies and a theoretical unreachable lower bound established

• Result represented as a ratio to the random baseline method

Mapping: For each task, add replicas randomly on available processors until reaching its reliability target

Scheduling: Randomly order replicas mapped on each processor and execute them in sequence and as soon as possible

1000 experiments randomly generated for each point on the graph



Ratio of energy consumption to the baseline of different mapping and scheduling ordering tasks criteria

sch map	deNR	inNR	deU	inU	random
deW	0.5655	0.5662	0.5655	0.5660	0.5663
inW	0.5631	0.5635	0.5630	0.5635	0.5635
deMinW	0.5658	0.5662	0.5657	0.5661	0.5665
inMinW	0.5637	0.5642	0.5637	0.5642	0.5641
deMaxW	0.5658	0.5664	0.5657	0.5663	0.5665
inMaxW	0.5629	0.5633	0.5629	0.5633	0.5633
random	0.5633	0.5639	0.5633	0.5638	0.5639

Reminder

Mapping ordering tasks criteria

- **deW/inW**: decreasing/increasing average WCET on all processors
- **deMinW/inMinW**: decreasing/increasing minimum WCET on all processors
- **deMaxW/inMaxW**: decreasing/increasing maximum WCET on all processors
- random: random ordering

Scheduling ordering tasks criteria

- **deNR/inNR**: decreasing/increasing number of replicas
- deU/inU: decreasing/increasing total utilization (sum up the values of c_{i,k}/p for all replicas)
- **random**: random ordering

Ordering task criteria do not critically influence energy consumption

 Focus on selecting processors strategies during the mapping phase, and on choosing primary and secondary replicas during the scheduling phase



strategy





(b) Comparing scheduling strategies when using deP as mapping strategy

Ratio of energy consumption using different mapping and scheduling strategies under big failure rate, when varying cor_{proc} , with basicWork = 0.3, $\beta_{b/w} = 1$, $\mathcal{R}_i = 0.95$ and $cor_{task} = 0.5$.

<u>Reminder</u>

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Mapping ordering processors criteria

- **inE**: increasing energy cost
- deR: decreasing reliability

 $-\frac{\log_{10}(1-R(\tau_i,m_k))}{\log_{10}(1-R(\tau_i,m_k))}$

- **deP**: decreasing ratio of $\frac{1}{E(\tau_i, m_k)}$
- random: random ordering

Scheduling primary replica choosing criteria

- **time**: choose the processor that can complete the replica the earliest
- energy: choose the processor that can execute the replica with the smallest dynamic energy

Scheduling secondary replica choosing criteria

- **time**: choose the processor whose start time can be the latest
- **energy**: choose the processor that can execute the replica with the largest dynamic energy
- Result less than 0.25 and close to lower bound when $cor_{proc} = 0$, ratio increases with cor_{proc}
- Mapping: deP performs better than, or similarly to the best strategy between deR and inE
- Scheduling: Little difference between our different scheduling criteria, time better when cor_{proc} ≠ 1 and energy better when cor_{proc} = 1

Experiments







(a) Comparing mapping strategies when using *time-time* as scheduling strategy

Ratio of energy consumption using different mapping and scheduling strategies under big failure rate when varying $\beta_{b/w}$, with *basicWork* = 0.3, $\mathcal{R}_i = 0.95$ and *cor*_{task} = 0.5.

Reminder

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Mapping ordering processors criteria

- inE: increasing energy cost
- deR: decreasing reliability

$\log_{10}(1-R(\tau_i,m_k))$

- **deP**: decreasing ratio of $\frac{1}{E(\tau_i, m_k)}$
- random: random ordering

Scheduling primary replica choosing criteria

- **time**: choose the processor that can complete the replica the earliest
- **energy**: choose the processor that can execute the replica with the smallest dynamic energy

Scheduling secondary replica choosing criteria

- **time**: choose the processor whose start time can be the latest
- energy: choose the processor that can execute the replica with the largest dynamic energy

 \blacklozenge Results are similar whatever the value of $\beta_{b/w}$

• Actual tasks execution time in $[\beta_{b/w}c_{i,k}, c_{i,k}]$, thus robustness of our heuristics





(a) Comparing mapping strategies when using *time-time* as scheduling strategy

Ratio of energy consumption using different mapping and scheduling strategies when varying *basicWork* and \mathcal{R}_i , under big failure rate, with $\beta_{b/w} = 1$ and $cor_{task} = 0.5$.

Reminder

Mapping ordering processors criteria

- inE: increasing energy cost
- deR: decreasing reliability

$\frac{\log_{10}(1-R(\tau_i,m_k))}{E(\tau_i,m_k)}$

- **deP**: decreasing ratio of $E(\tau_i, m_k)$
- random: random ordering

Scheduling primary replica choosing criteria

- **time**: choose the processor that can complete the replica the earliest
- **energy**: choose the processor that can execute the replica with the smallest dynamic energy

Scheduling secondary replica choosing criteria

- **time**: choose the processor whose start time can be the latest
- **energy**: choose the processor that can execute the replica with the largest dynamic energy

Mapping: deP has always better or similar performance than the best of deR and inE

Scheduling: similar performance on all criteria except random

Little difference between our strategies and the lower bound, difference of 10% in the worst case



- Save more than 40% of energy compared to baseline, except in the high cor_{proc} case, ratio can be as low as 20% in the best case
- deP method is the best processor ordering during the mapping phase
- All primary-secondary replica choosing heuristic performs well, "time" good primary replica choosing criteria when cor_{proc} ≈1, "energy" other cases
- Performance of the best heuristics is only 17.0% higher than the lower bound in the worst case, the median value is only 3.5% and the average value is only 4.3% higher
- We can confidently conclude that our best strategies perform remarkably well over the whole experimental setting





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Problem	Execute periodic real-time tasks on an heterogeneous platform, with objectives to minimizing the energy consumption, guaranteeing some reliability thresholds, and meeting all deadlines
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Solution	A multi-criteria mapping-scheduling heuristic
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Experiments	Our best heuristics always achieve good performance, which is very close to the lower bound
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THANK YOU FOR LISTENING !